

What I learn today, prepares me for tomorrow.

# **Calculation Policy**

2024-2025

Policy	Written:	Review Due:	Person Responsible:
Location:			
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Policy Library	2023	2025	SLT
			All staff
			Strategic Committee

The following pages show the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

As a school we use a range of resources to support our teaching in mathematics, we have subscriptions to White Rose, Numicon and NCFE to support our learners. Our students are taught in ability groups to suit their ability and understanding.

#### **KEY STAGE 1**

Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction.

**Key language:** whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table

Addition and subtraction: Children first learn to connect addition and subtraction with counting, but they soon develop two very important skills: an understanding of parts and wholes, and an understanding of unitising 10s, to develop efficient and effective calculation strategies based on known number bonds and an increasing awareness of place value. Addition and subtraction are taught in a way that is interlinked to highlight the link between the two operations. A key idea is that children will select methods and approaches based on their number sense. For example, in Year 1, when faced with 15 - 3 and 15 - 13, they will adapt their ways of approaching the calculation appropriately. The teaching should always emphasise the importance of mathematical thinking to ensure accuracy and flexibility of approach, and the importance of using known number facts to harness their recall of bonds within 20 to support both addition and subtraction methods.

In Year 2, they will start to see calculations presented in a column format, although this is not expected to be formalised until KS2. We show the column method in Year 2 as an option; teachers may not wish to include it until Year 3.

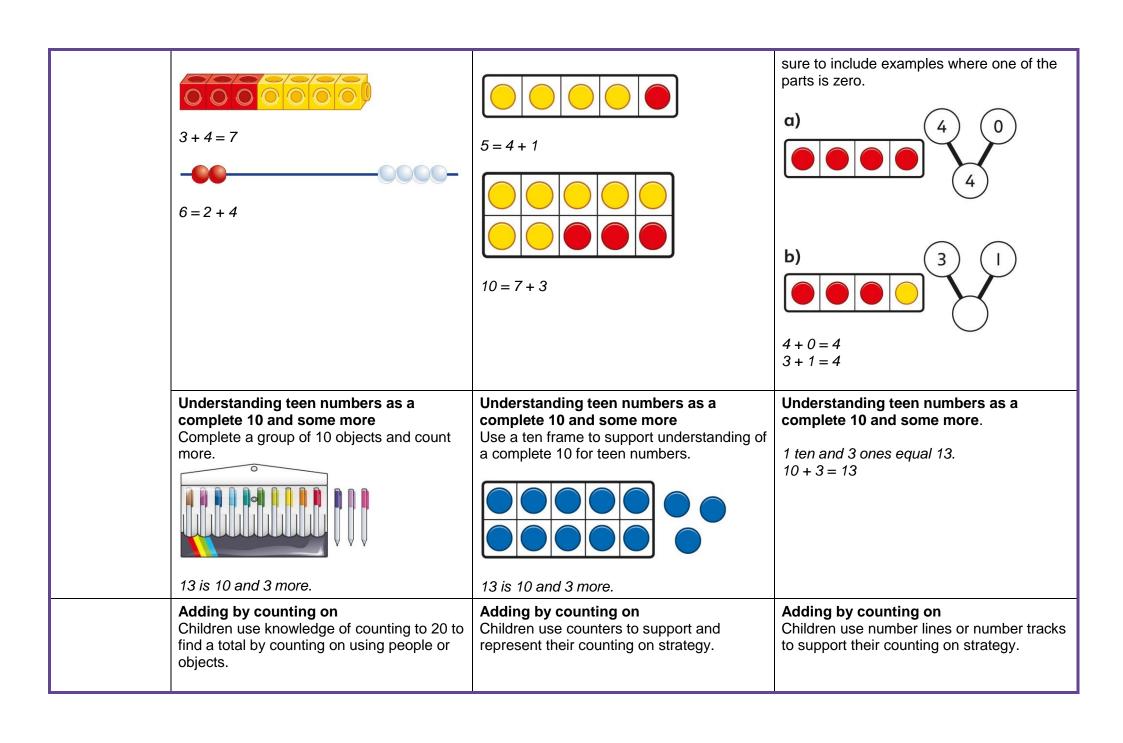
**Multiplication and division:** Children develop an awareness of equal groups and link this with counting in equal steps, starting with 2s, 5s and 10s. In Year 2, they learn to connect the language of equal groups with the mathematical symbols for multiplication and division.

They learn how multiplication and division can be related to repeated addition and repeated subtraction to find the answer to the calculation. In this key stage, it is vital that children explore and experience a variety of strong images and manipulative representations of equal groups, including concrete experiences as well as abstract calculations.

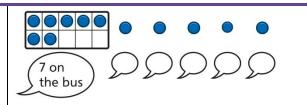
Children begin to recall some key multiplication facts, including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.

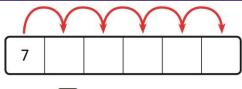
**Fractions:** In Year 1, children encounter halves and quarters, and link this with their understanding of sharing. They experience key spatial representations of these fractions, and learn to recognise examples and non-examples, based on their awareness of equal parts of a whole. In Year 2, they develop an awareness of unit fractions and experience non-unit fractions, and they learn to write them and read them in the common format of numerator and denominator.

	Year 1				
	Concrete	Pictorial	Abstract		
Year 1 Addition	Counting and adding more Children add one more person or object to a group to find one more.	Counting and adding more Children add one more cube or counter to a group to represent one more.	Counting and adding more Use a number line to understand how to link counting on with finding one more.		
		00000	one more 0 1 2 3 4 5 6 7 8 9 10		
		One more than 4 is 5.	One more than 6 is 7. 7 is one more than 6.		
			Learn to link counting on with adding more than one.  1		
	Understanding part-part-whole relationship Sort people and objects into parts and understand the relationship with the whole.	Understanding part-part-whole relationship Children draw to represent the parts and understand the relationship with the whole.	Understanding part-part-whole relationship Use a part-whole model to represent the numbers.  6 4 4 = 10		
	The parts are 2 and 4. The whole is 6.	The parts are 1 and 5. The whole is 6.	6 + 4 = 10		
	Knowing and finding number bonds within 10 Break apart a group and put back together to find and form number bonds.	Knowing and finding number bonds within 10 Use five and ten frames to represent key number bonds.	Knowing and finding number bonds within 10 Use a part-whole model alongside other representations to find number bonds. Make		









Adding the 1s

#### Adding the 1s

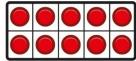
Children use bead strings to recognise how to add the 1s to find the total efficiently.

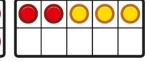


$$2 + 3 = 5$$
  
 $12 + 3 = 15$ 

### Adding the 1s

Children represent calculations using ten frames to add a teen and 1s.





$$3 + 5 = 8$$
  
So,  $13 + 5 = 18$ 

## 2 + 3 = 512 + 3 = 15

### Bridging the 10 using number bonds

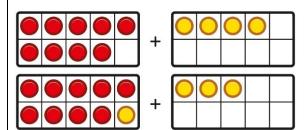
Children use a bead string to complete a 10 and understand how this relates to the addition.



7 add 3 makes 10. So, 7 add 5 is 10 and 2 more.

# Bridging the 10 using number bonds

Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.

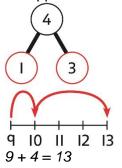


### Bridging the 10 using number bonds

Use a part-whole model and a number line to support the calculation.

Children recognise that a teen is made from

a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.



# Year 1 Subtraction

#### Counting back and taking away

Children arrange objects and remove to find how many are left.

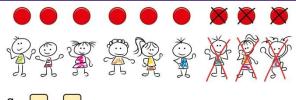


#### Counting back and taking away

Children draw and cross out or use counters to represent objects from a problem.

#### Counting back and taking away

Children count back to take away and use a number line or number track to support the method. 1 less than 6 is 5. 6 subtract 1 is 5.





There are children left.



$$9 - 3 = 6$$

# Finding a missing part, given a whole and a part

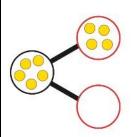
Children separate a whole into parts and understand how one part can be found by subtraction.



$$8 - 5 = ?$$

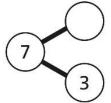
# Finding a missing part, given a whole and a part

Children represent a whole and a part and understand how to find the missing part by subtraction.



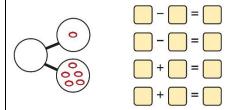
# Finding a missing part, given a whole and a part

Children use a part-whole model to support the subtraction to find a missing part.



7 - 3 = ?

Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.

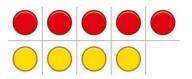


### Finding the difference

Arrange two groups so that the difference between the groups can be worked out.

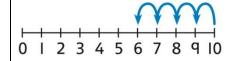
#### Finding the difference

Represent objects using sketches or counters to support finding the difference.



#### Finding the difference

Children understand 'find the difference' as subtraction.



	1	1	7	
12		65		

8 is 2 more than 6. 6 is 2 less than 8. The difference between 8 and 6 is 2. 5 - 4 = 1

The difference between 5 and 4 is 1.

10 - 4 = 6

The difference between 10 and 6 is 4.

#### **Subtraction within 20**

Understand when and how to subtract 1s efficiently.

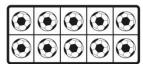
Use a bead string to subtract 1s efficiently.



$$5-3=2$$
  
 $15-3=12$ 

#### **Subtraction within 20**

Understand when and how to subtract 1s efficiently.



$$5 - 3 = 2$$
  
 $15 - 3 = 12$ 

#### Subtraction within 20

Understand how to use knowledge of bonds within 10 to subtract efficiently.

$$5 - 3 = 2$$
  
 $15 - 3 = 12$ 

### **Subtracting 10s and 1s**

For example: 18 - 12

Subtract 12 by first subtracting the 10, then the remaining 2.



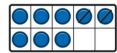
First subtract the 10, then take away 2.

#### **Subtracting 10s and 1s**

For example: 18 - 12

Use ten frames to represent the efficient method of subtracting 12.





First subtract the 10, then subtract 2.

## Subtracting 10s and 1s

Use a part-whole model to support the calculation.



# **Subtraction bridging 10 using number bonds**

For example: 12 - 7

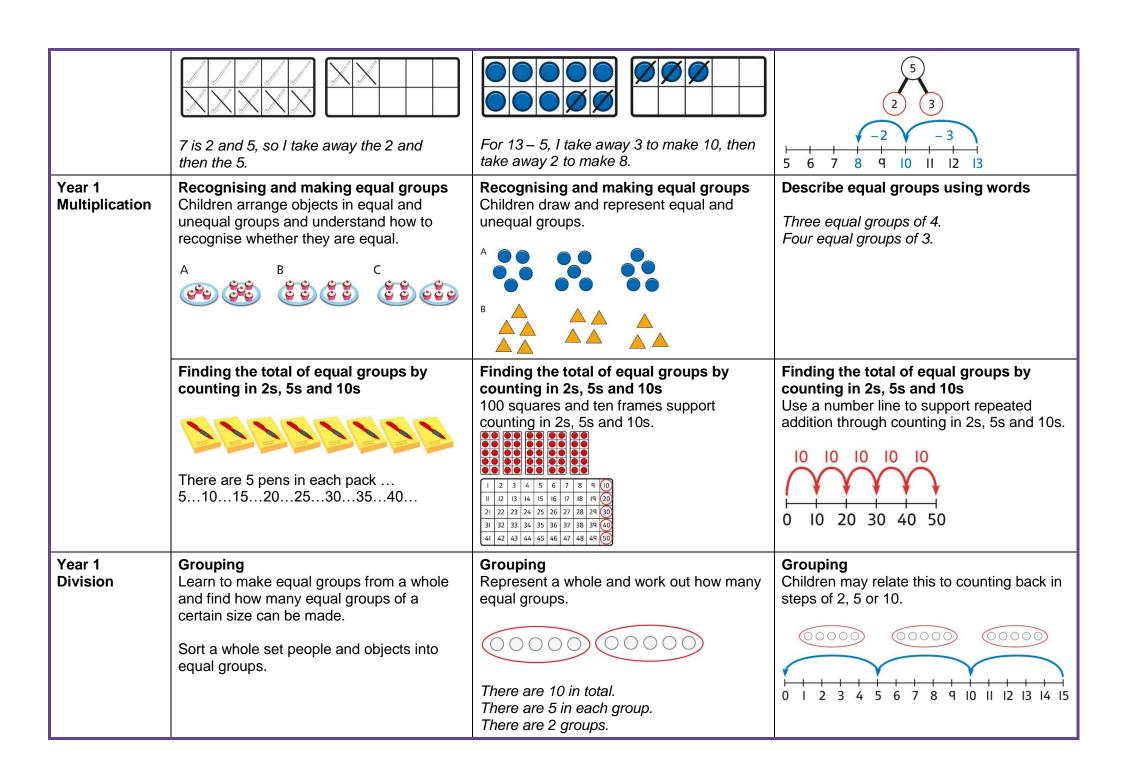
Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.

# **Subtraction bridging 10 using number bonds**

Represent the use of bonds using ten frames.

# **Subtraction bridging 10 using number bonds**

Use a number line and a part-whole model to support the method.

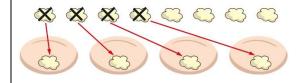




There are 10 children altogether. There are 2 in each group. There are 5 groups.

#### **Sharing**

Share a set of objects into equal parts and work out how many are in each part.



### **Sharing**

Sketch or draw to represent sharing into equal parts. This may be related to fractions.



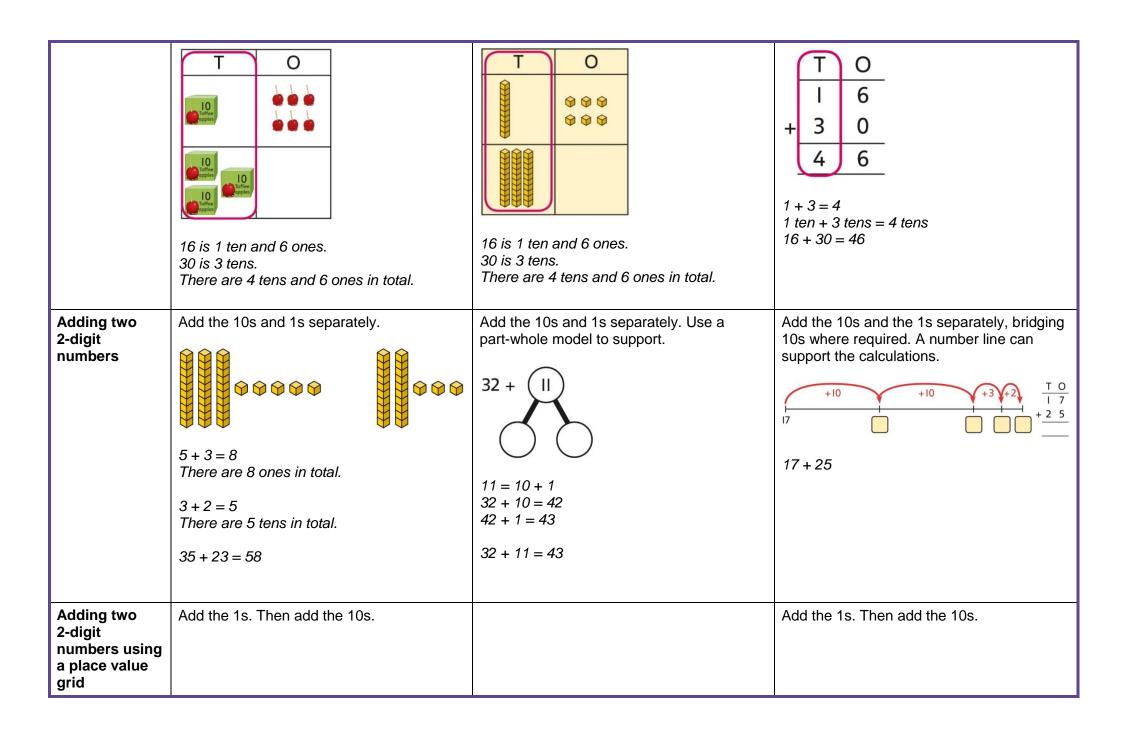
#### **Sharing**

10 shared into 2 equal groups gives 5 in each group.

	Year 2				
	Concrete	Pictorial	Abstract		
Year 2 Addition					
Understanding 10s and 1s	Bundle straws to understand unitising of 10s.	Understand 10s and 1s equipment, and link with visual representations on ten frames.	Represent numbers on a place value grid, using equipment or numerals.  Tens Ones  3 2  Tens Ones 4 3		
Adding 10s	Use known bonds and unitising to add 10s.  I know that $4 + 3 = 7$ .  So, I know that 4 tens add 3 tens is 7 tens.	Use known bonds and unitising to add 10s.  I know that $4 + 3 = 7$ .  So, I know that $4$ tens add $3$ tens is $7$ tens.	Use known bonds and unitising to add 10s. $4+3=$ $4+3=7$ $4 tens + 3 tens = 7 tens$ $40+30=70$		
Adding a 1-digit number to a 2-digit	Add the 1s to find the total. Use known bonds within 10.	Add the 1s.	Add the 1s.  Understand the link between counting on and using known number facts. Children		

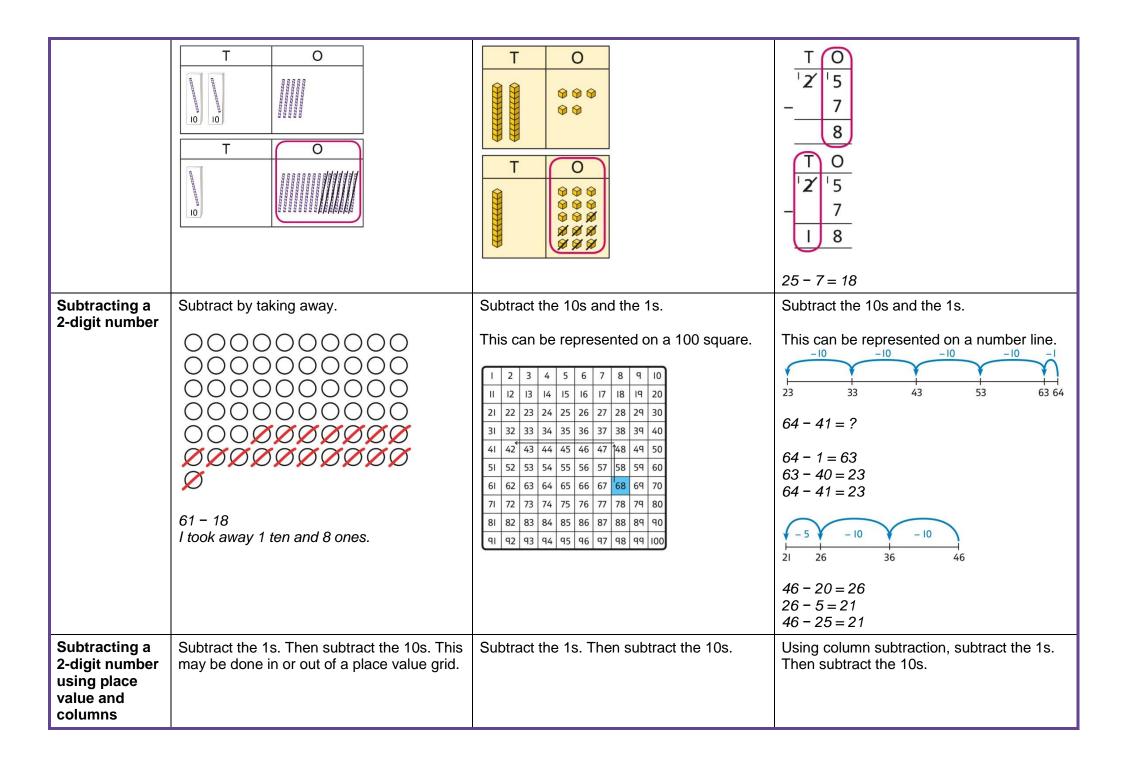
number not bridging a 10	41 is 4 tens and 1 one. 41 add 6 ones is 4 tens and 7 ones.  This can also be done in a place value grid.	+	should be encouraged to use known number bonds to improve efficiency and accuracy.  1
Adding a 1-digit number to a 2-digit number bridging 10	There are 4 tens and 5 ones. I need to add 7. I will use 5 to complete a 10, then add 2 more.	Complete a 10 using number bonds.	Complete a 10 using number bonds.  7 5 2 43 44 45 46 47 48 49 50 51 52 53 7 = 5 + 2 45 + 5 + 2 = 52
Adding a 1-digit number to a 2-digit number using exchange	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.

Adding a multiple of 10 to a 2-digit number	Add the 10s and then recombine.  27 is 2 tens and 7 ones. 50 is 5 tens.  There are 7 tens in total and 7 ones. So, 27 + 50 is 7 tens and 7 ones.	T O  Add the 10s and then recombine.  Add the 10s and 6 ones.  66 is 6 tens and 6 ones.  66 + 10 = 76  A 100 square can support this understanding.  1 2 3 4 5 6 7 8 9 10 11 120 20 21 21 22 23 24 25 26 27 28 29 30 31 33 33 34 35 36 37 38 39 40 40 41 42 43 44 45 46 47 48 47 50 55 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 47 68 64 70 71 71 72 73 74 78 80 80 81 82 83 84 85 88 67 88 89 90 90 91 91 91 91 91 91 91 91 91 91 91 91 91	Add the 10s and then recombine. $37 + 20 = ?$ $30 + 20 = 50$ $50 + 7 = 57$ $37 + 20 = 57$
Adding a multiple of 10 to a 2-digit number using columns	Add the 10s using a place value grid to support.	Add the 10s using a place value grid to support.	Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value.



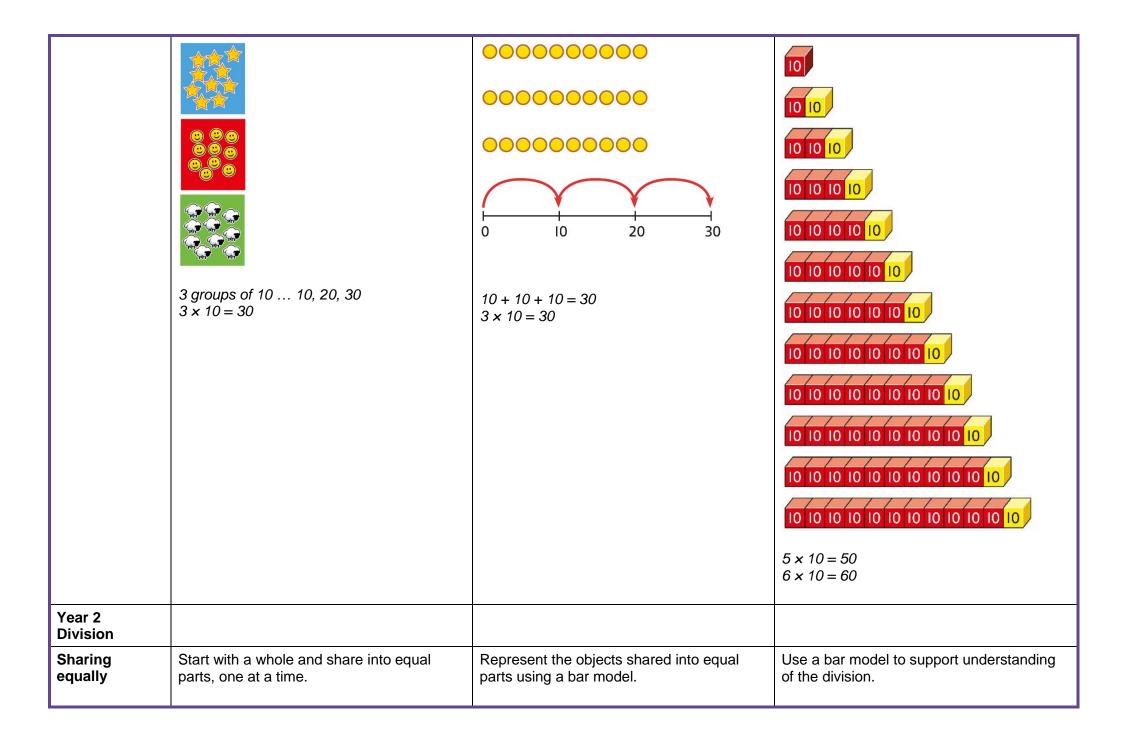
	Tens Ones  Tens Ones  Tens Ones  Tens Ones  Tens Ones		T O 3 2 + 1 4 6 6 T O 3 2 + 1 4 4 6
Adding two 2-digit numbers with exchange	Add the 1s. Exchange 10 ones for a ten. Then add the 10s.  Tens Ones  q  Tens Ones  q  Tens Ones		Add the 1s. Exchange 10 ones for a ten. Then add the 10s.  TO 3 6 + 2 9 5 TO 3 6 + 2 9 6 5
Year 2 Subtraction			
Subtracting multiples of 10	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.

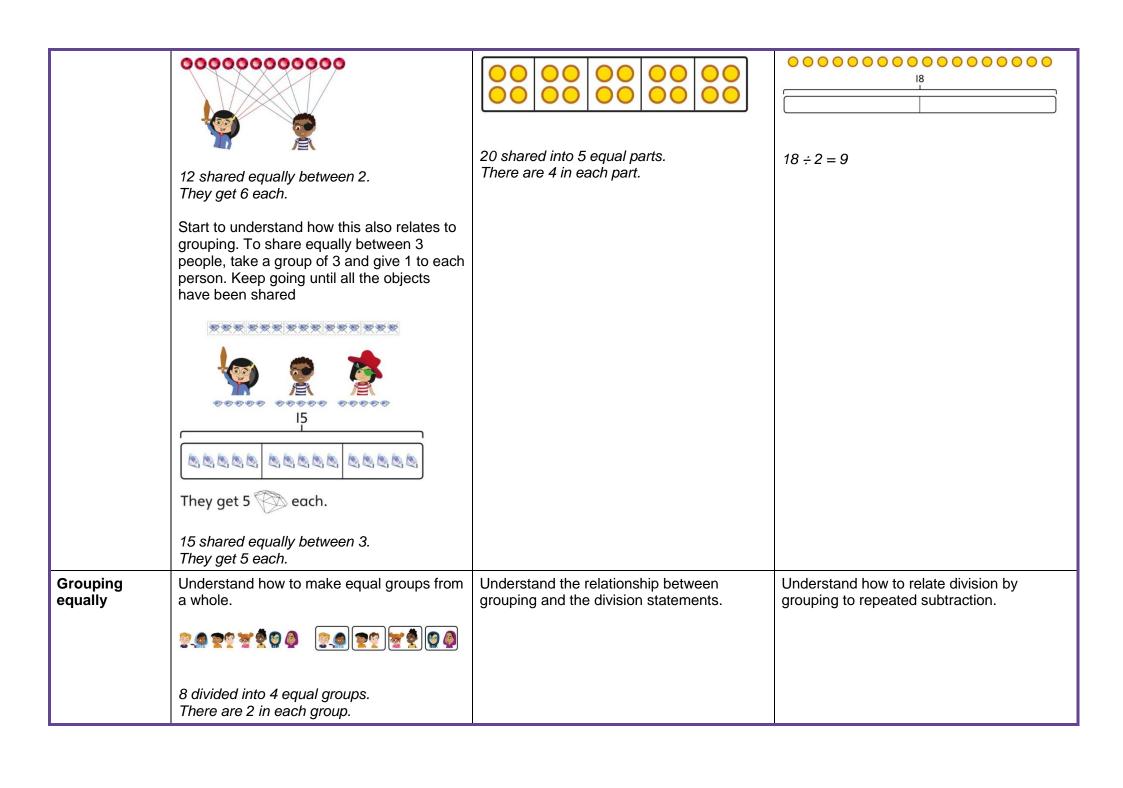
		100	7 70 70 20 50
	8 subtract 6 is 2. So, 8 tens subtract 6 tens is 2 tens.	10 - 3 = 7 So, 10 tens subtract 3 tens is 7 tens.	7 tens subtract 5 tens is 2 tens. 70 - 50 = 20
Subtracting a single-digit number	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds.  30 31 32 33 34 35 36 37 38 39 40
	T O	T O	$ \begin{array}{c cccc}  & T & O \\ \hline 3 & 9 \\ \hline  & 3 & 6 \\ \hline  & 39 - 3 = 6 \\ \hline  & 39 - 3 = 36 \end{array} $
Subtracting a single-digit number bridging 10	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.  -4  16 17 18 19 20 21 22 23 24 25 26
	35 - 6 I took away 5 counters, then 1 more.	35 - 6 First, I will subtract 5, then 1.	24 - 6 = ? 24 - 4 - 2 = ?
Subtracting a single-digit number using exchange	Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.	Exchange 1 ten for 10 ones.	Exchange 1 ten for 10 ones.

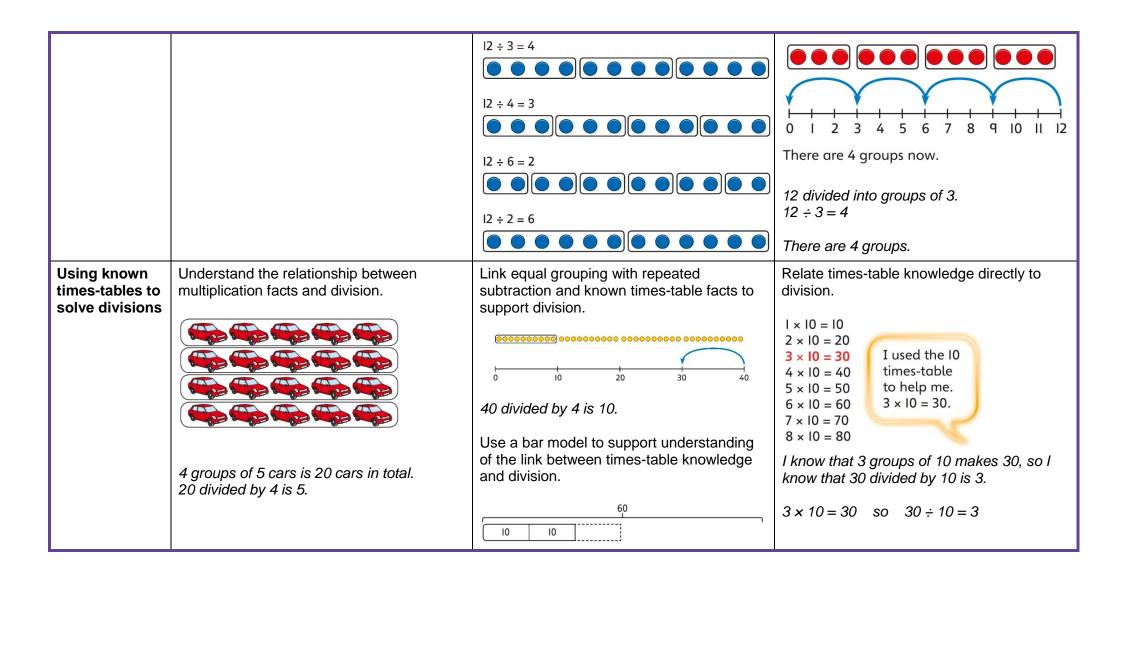


	T O O O O O O O O O O O O O O O O O O O	Tens Ones	T O 4 5 - I 2 3 T O 4 5 - I 2 3 3 3
Subtracting a 2-digit number with exchange		Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.  Tens Ones  Tens Ones  Tens Ones  Tens Ones  Tens Ones	Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 1os.  TO 45 -27 TO 3/4   5 -27 TO 3/4   5 -27 8 TO 3/4   5 -27 8 TO 3/4   5 -27 8
Multiplication			
Equal groups and repeated addition	Recognise equal groups and write as repeated addition and as multiplication.	Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.	Use a number line and write as repeated addition and as multiplication.

	3 groups of 5 chairs 15 chairs altogether	3 groups of 5 15 in total	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Using arrays to represent multiplication and support understanding	Understand the relationship between arrays, multiplication and repeated addition.	Understand the relationship between arrays, multiplication and repeated addition.   4 groups of 5 5 groups of 5	Understand the relationship between arrays, multiplication and repeated addition. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Understanding commutativity	Use arrays to visualise commutativity.  I can see 6 groups of 3. I can see 3 groups of 6.	Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.  This is 2 groups of 6 and also 6 groups of 2.	Use arrays to visualise commutativity. $4+4+4+4+4+4=20$ $5+5+5+5=20$ $4 \times 5 = 20 \text{ and } 5 \times 4 = 20$
Learning ×2, ×5 and ×10 table facts	Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.	Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.	Understand how the times-tables increase and contain patterns.







#### **KEY STAGE 2**

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process. alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns. By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively. Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.

Children develop column methods to support multiplications in these cases.

For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

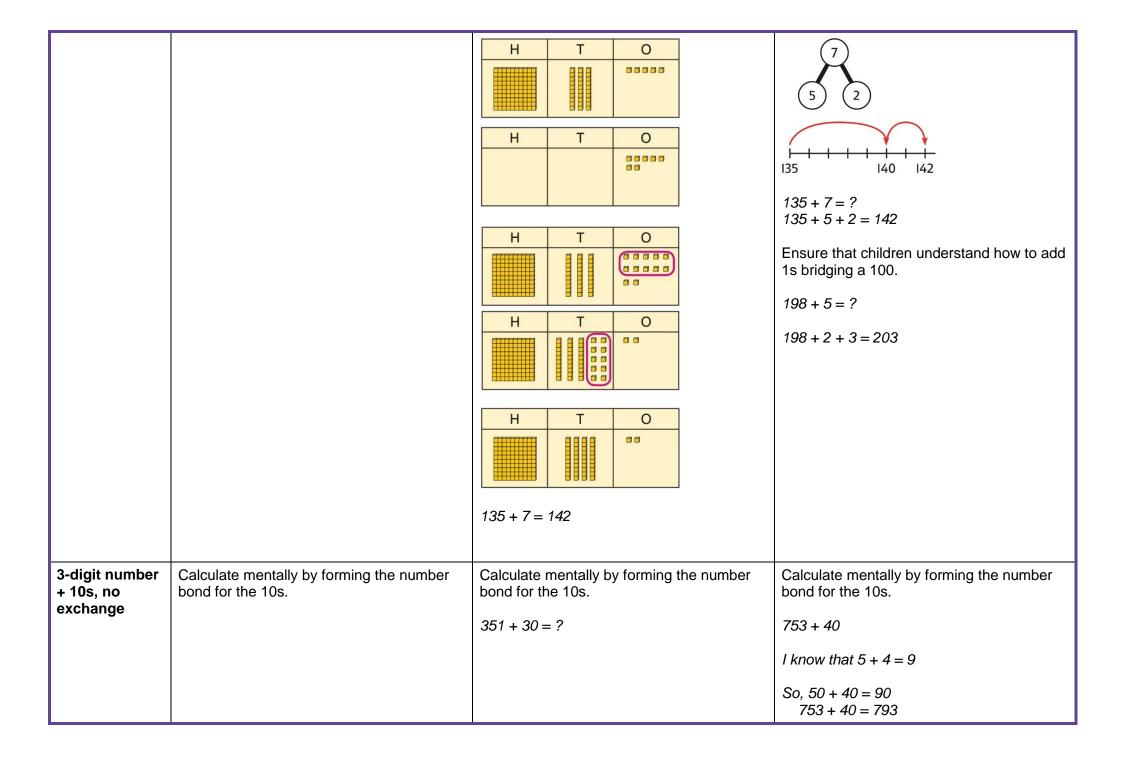
Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

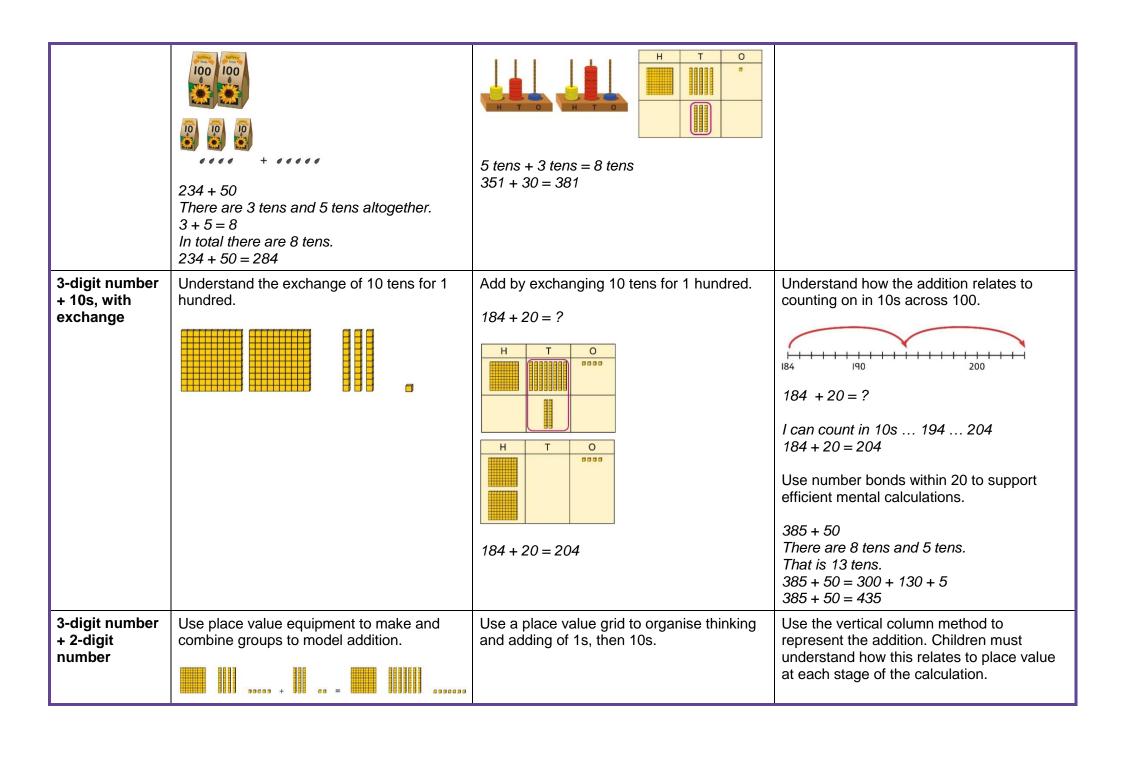
in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.

		Year 3	
	Concrete	Pictorial	Abstract
Year 3 Addition			
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens.  Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.
	* * * * * * * * * * * * * * * * * * *		500 400 200 0
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use equipment to represent numbers to 1,000.	Represent the parts of numbers to 1,000 using a part-whole model.
	100 200 210 211 212 213 214 215	200 240 241	215 = 200 + 10 + 5
		Use a place value grid to support the structure of numbers to 1,000.  Place value counters are used alongside	Recognise numbers to 1,000 represented on a number line, including those between intervals.
		other equipment. Children should understand how each counter represents a different unitised amount.	
Adding 100s	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.
			Represent the addition on a number line.

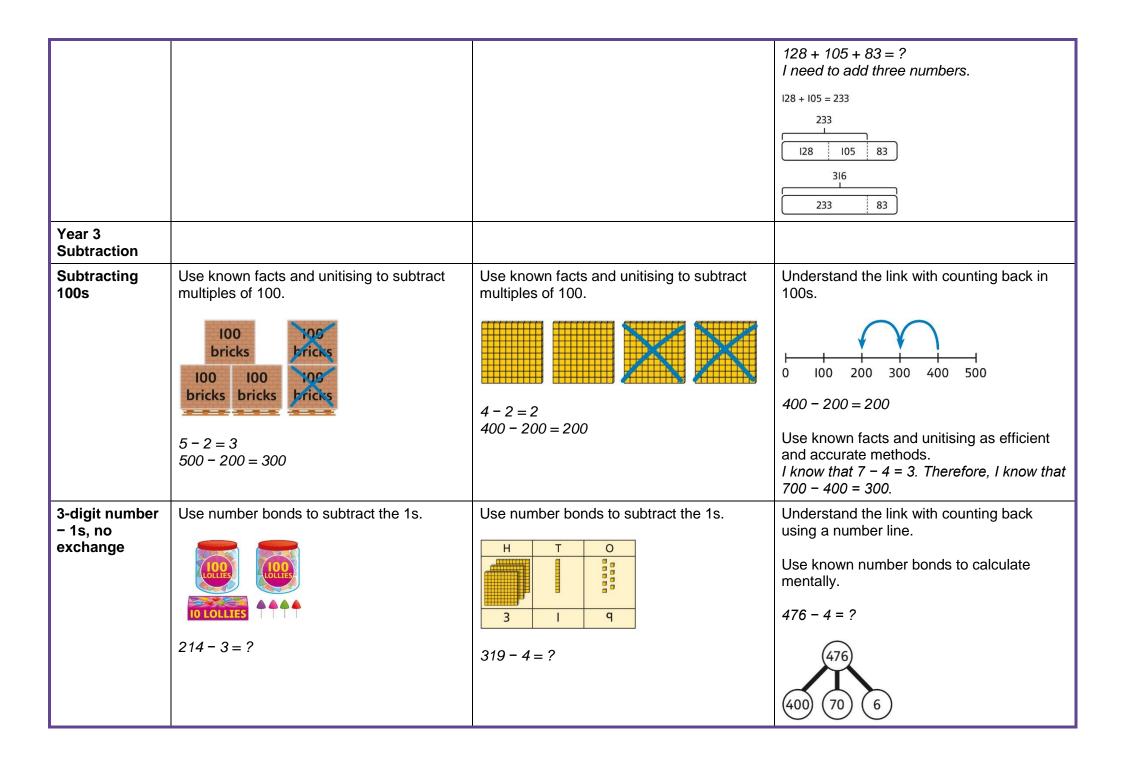
	100 bricks $100$ bricks $100$ bricks $3+2=5$ $3  hundreds + 2  hundreds = 5  hundreds$ $300 + 200 = 500$	3 + 4 = 7 3 hundreds + 4 hundreds = 7 hundreds 300 + 400 = 700	Use a part-whole model to support unitising. $3 + 2 = 5$ $300 + 200 = 500$
3-digit number + 1s, no exchange or bridging	Use number bonds to add the 1s.  214 + 4 = ?  Now there are $4 + 4$ ones in total. $4 + 4 = 8$ 214 + 4 = 218	Use number bonds to add the 1s.  H T O Use number bonds to add the Is. $5+4=9$ $245+4$ $5+4=9$ $245+4=249$	Understand the link with counting on. $245 + 4$ $245 + 4$ Use number bonds to add the 1s and understand that this is more efficient and less prone to error. $245 + 4 = ?$ I will add the 1s. $5 + 4 = 9$ So, $245 + 4 = 249$
3-digit number + 1s with exchange	Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.  Children should explore this using unitised objects or physical apparatus.	Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.	Understand how to bridge by partitioning to the 1s to make the next 10.





3-digit number + 2-digit number, exchange required	Use place value equipment to model addition and understand where exchange is required.  Use place value counters to represent 154 + 72.  Use this to decide if any exchange is required.  There are 5 tens and 7 tens. That is 12 tens so I will exchange.	Represent the required exchange on a place value grid using equipment.  275 + 16 = ?  H T O  H T O  275 + 16 = 291  Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value. Children should be encouraged at every stage to select methods that are accurate and efficient.	Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.  H T O
3-digit number + 3-digit number, no exchange	Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.  326 + 541 is represented as:	Represent the place value grid with equipment to model the stages of column addition.	Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.

	3 2 6 5 4 I		
3-digit number + 3-digit number, exchange required	Use place value equipment to enact the exchange required.	Model the stages of column addition using place value equipment on a place value grid.	Use column addition, ensuring understanding of place value at every stage of the calculation.  H T O  1 2 6  + 2 1 7
	There are 13 ones. I will exchange 10 ones for 1 ten.	H T O	$ \frac{\frac{H \text{ T O}}{1 \text{ 2 6}}}{\frac{1 \text{ 2 6}}{4 \text{ 3}}} $
		H T O	H T O 1 2 6 +2 1 7 3 4 3
			126 + 217 = 343 Note: Children should also study examples where exchange is required in more than one column, for example 185 + 318 = ?
Representing addition problems, and selecting appropriate	Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps.	Children understand and create bar models to represent addition problems.  275 + 99 = ?	Use representations to support choices of appropriate methods.
methods	These representations will help them to select appropriate methods.	$ \begin{array}{c c} 374 \\ \hline 275 & qq \end{array} $ $ 275 + 99 = 374 $	I will add 100, then subtract 1 to find the solution.



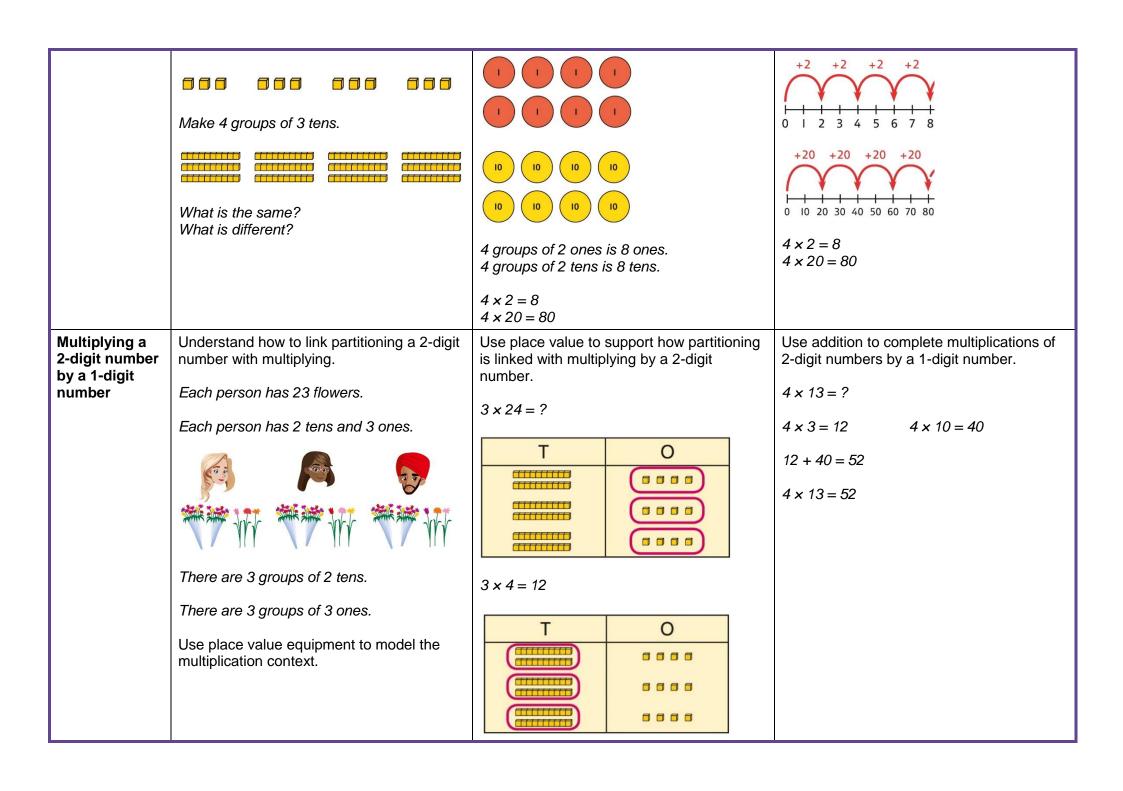
3-digit number – 1s, exchange or bridging required	Understand why an exchange is necessary by exploring why 1 ten must be exchanged.  Use place value equipment.	9-4=5 $319-4=315$ Represent the required exchange on a place value grid. $151-6=?$ H T O	6 - 4 = 2 476 - 4 = 472  Calculate mentally by using known bonds.  151 - 6 = ?  151 - 1 - 5 = 145
3-digit number – 10s, no exchange	Subtract the 10s using known bonds.  381 - 10 = ?  8 tens with 1 removed is 7 tens.  381 - 10 = 371	Subtract the 10s using known bonds.  H T O  8 tens - 1 ten = 7 tens 381 - 10 = 371	Use known bonds to subtract the 10s mentally. $372 - 50 = ?$ $70 - 50 = 20$ So, $372 - 50 = 322$

3-digit number – 10s, exchange or	Use equipment to understand the exchange of 1 hundred for 10 tens.	Represent the exchange on a place value grid using equipment.	Understand the link with counting back on a number line.
bridging required		210 - 20 = ?  H T O  I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.  H T O  210 - 20 = 190	Use flexible partitioning to support the calculation. $235 - 60 = ?$ $235 = 100 + 130 + 5$ $235 - 60 = 100 + 70 + 5$ $= 175$
3-digit number  – up to 3-digit number	Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.	Represent the calculation on a place value grid.  H T O D D D D D D D D D D D D D D D D D D	Use column subtraction to calculate accurately and efficiently.  H T O       q q q    - 3 5 2
3-digit number  – up to 3-digit number,	Use equipment to enact the exchange of 1 hundred for 10 tens, and 1 ten for 10 ones.	Model the required exchange on a place value grid.  175 - 38 = ?	Use column subtraction to work accurately and efficiently.

exchange required	H T O H T O H T O NAME  H T O NAME  H T O NAME  NAME	H T O I 6 1 1 5 1 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1
Representing subtraction problems	Use bar models to represent subtractions.  'Find the difference' is represented as two bars for comparison.  Team A 454  Team B 128 ?  Bar models can also be used to show that a part must be taken away from the whole.	Children use alternative representations to check calculations and choose efficient methods.  Children use inverse operations to check additions and subtractions. The part-whole model supports understanding.  I have completed this subtraction. 525 - 270 = 255 I will check using addition.

Year 3 Multiplication			525 270 (255) H T O 2 7 0 + 2 5 5 5 2 5
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and nonexamples using objects.  Children recognise that arrays can be used to model commutative multiplications.  I can see 3 groups of 8. I can see 8 groups of 3.	Children recognise that arrays demonstrate commutativity.  This is 3 groups of 4. This is 4 groups of 3.	Children understand the link between repeated addition and multiplication. $ \begin{array}{cccccccccccccccccccccccccccccccccc$
Using commutativity to support	Understand how to use times-tables facts flexibly.	Understand how times-table facts relate to commutativity.	Understand how times-table facts relate to commutativity.

understanding of the times- tables	There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls.  I can use 6 × 4 = 24 to work out both totals.	6 x 4 = 24 4 x 6 = 24	I need to work out 4 groups of 7.  I know that 7 x 4 = 28  so, I know that  4 groups of 7 = 28  and 7 groups of 4 = 28.
Understanding and using ×3, ×2, ×4 and ×8 tables.	Children learn the times-tables as 'groups of', but apply their knowledge of commutativity.  I can use the x3 table to work out how many keys. I can also use the x3 table to work out how many batteries.	Children understand how the x2, x4 and x8 tables are related through repeated doubling.	Children understand the relationship between related multiplication and division facts in known times-tables. $2 \times 5 = 10$ $5 \times 2 = 10$ $10 \div 5 = 2$ $10 \div 2 = 5$
Using known facts to multiply 10s, for example 3 × 40	Explore the relationship between known times-tables and multiples of 10 using place value equipment.  Make 4 groups of 3 ones.	Understand how unitising 10s supports multiplying by multiples of 10.	Understand how to use known times-tables to multiply multiples of 10.



	000
	333
A	666
3	000

There are 3 groups of 2 tens.

3	x	20	=	60
J	$\sim$	20	_	$\mathbf{o}$

$$60 + 12 = 72$$

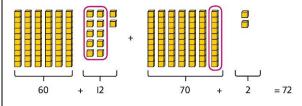
$$3 \times 24 = 72$$

## Multiplying a 2-digit number by a 1-digit number, expanded column method

Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.

$$3 \times 24 = ?$$

$$3 \times 20 = 60$$
  
 $3 \times 4 = 12$ 

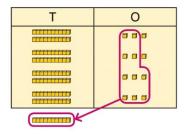


 $3 \times 24 = 60 + 12$  $3 \times 24 = 70 + 2$ 

$$3 \times 24 = 72$$

Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.

$$4 \times 23 = ?$$



Т	0
	6 6

$$4 \times 23 = 92$$

Children may write calculations in expanded column form, but must understand the link with place value and exchange.

Children are encouraged to write the expanded parts of the calculation separately.

Т	0
	00000
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	0 0 0 0 0

$$5 \times 28 = ?$$

Year 3 Division		T O  O O O O O O O O O O O O O O O O O O	
Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions.  24 divided into groups of 8. There are 3 groups of 8.	Use knowledge of known times-tables to calculate divisions.	Use knowledge of known times-tables to calculate divisions.  I need to work out 30 shared between 5.  I know that $6 \times 5 = 30$ so I know that $30 \div 5 = 6$ .  A bar model may represent the relationship between sharing and grouping. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

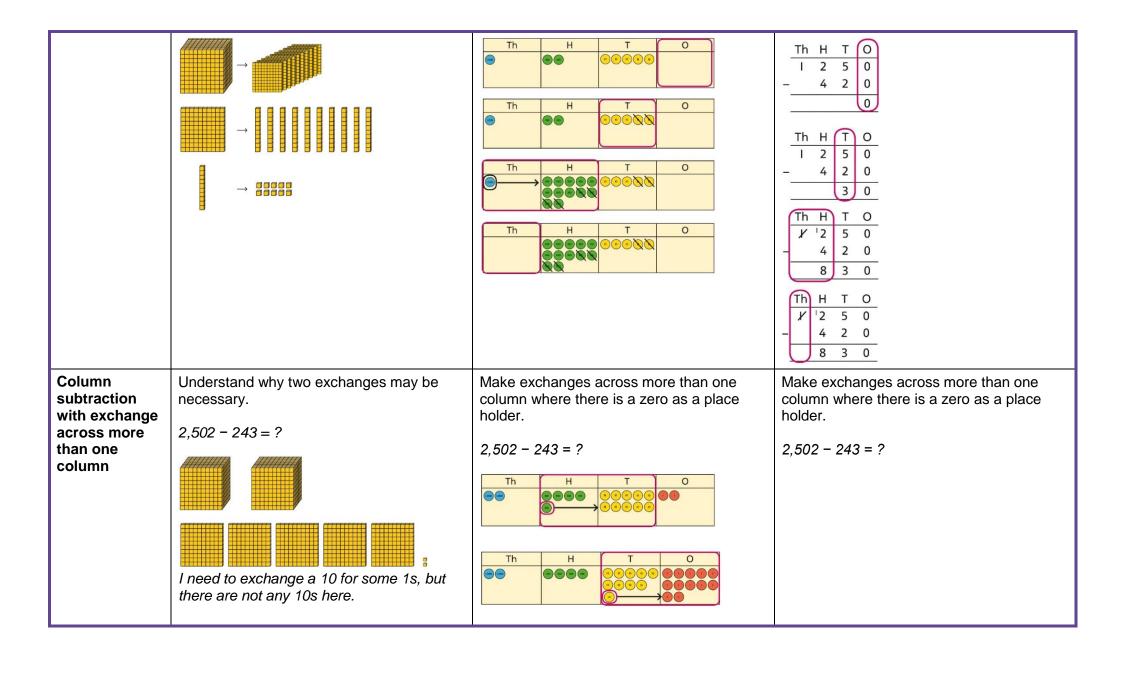
-			
			$24 \div 8 = 3$ $\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.  There are 13 sticks in total. There are 3 groups of 4, with 1 remainder.	Use images to explain remainders.  •••••••••••••••••••••••••••••••••••	Understand that the remainder is what cannot be shared equally from a set. $22 \div 5 = ?$ $3 \times 5 = 15$ $4 \times 5 = 20$ $5 \times 5 = 25 \dots$ this is larger than 22 So, $22 \div 5 = 4$ remainder 2
Using known facts to divide multiples of 10	Use place value equipment to understand how to divide by unitising.  Make 6 ones divided by 3.  Now make 6 tens divided by 3.  What is the same? What is different?	Divide multiples of 10 by unitising.  12 tens shared into 3 equal groups. 4 tens in each group.	Divide multiples of 10 by a single digit using known times-tables. $180 \div 3 = ?$ $180 \text{ is } 18 \text{ tens.}$ $18 \text{ divided by } 3 \text{ is } 6.$ $18 \text{ tens divided by } 3 \text{ is } 6 \text{ tens.}$ $18 \div 3 = 6$ $180 \div 3 = 60$
2-digit number divided by 1-digit number, no remainders	Children explore dividing 2-digit numbers by using place value equipment.	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate.

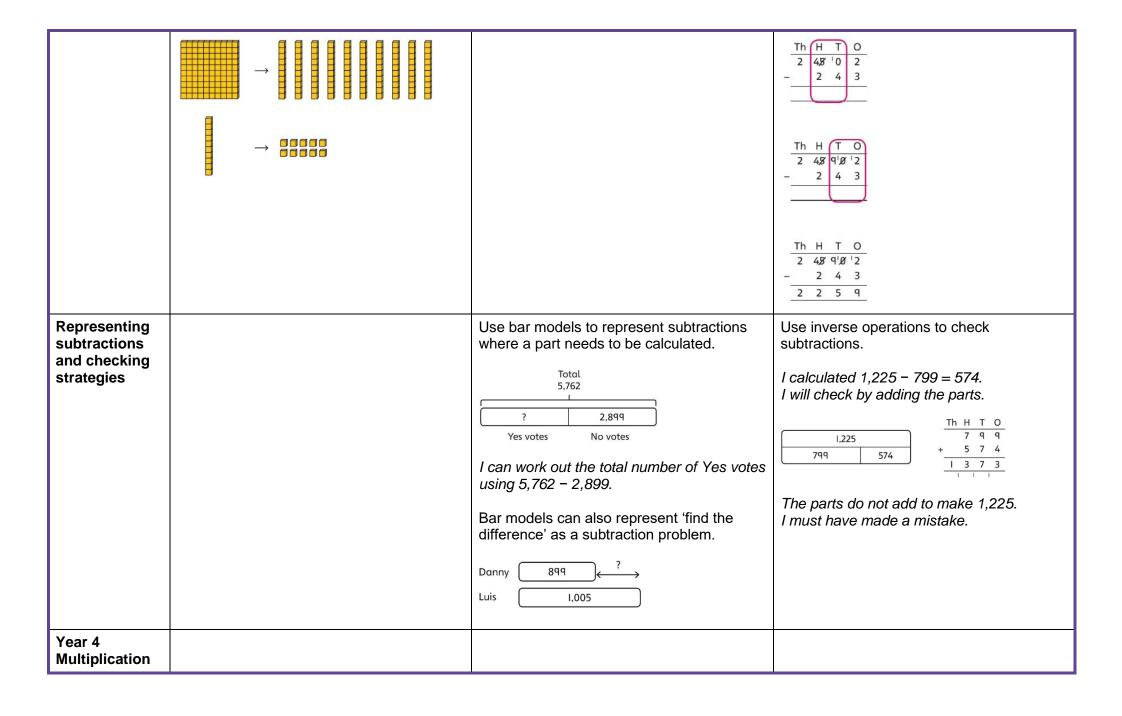
	### ### ##############################	I need to partition 42 differently to divide by 3. $42 = 30 + 12$	$60 \div 2 = 30$ $8 \div 2 = 4$ 30 + 4 = 34 $68 \div 2 = 34$ Children partition flexibly to divide where appropriate. $42 \div 3 = ?$ 42 = 40 + 2 I need to partition 42 differently to divide by 3. 42 = 30 + 12 $30 \div 3 = 10$ $12 \div 3 = 4$ 10 + 4 = 14 $42 \div 3 = 14$
2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder.  Make 29 from place value equipment. Share it into 2 equal groups.  There are two groups of 14 and 1 remainder.	$42 \div 3 = 14$ Use place value equipment to understand the concept of remainder in division. $29 \div 2 = ?$ $29 \div 2 = 14 \text{ remainder 1}$	Partition to divide, understanding the remainder in context.  67 children try to make 5 equal lines.  67 = $50 + 17$ $50 \div 5 = 10$ 17 $\div 5 = 3$ remainder 2 $67 \div 5 = 13$ remainder 2 There are 13 children in each line and 2 children left out.

	Year 4				
	Concrete	Pictorial	Abstract		
Year 4 Addition					
Understanding numbers to 10,000	Use place value equipment to understand the place value of 4-digit numbers.  4 thousands equal 4,000.  1 thousand is 10 hundreds.	Represent numbers using place value counters once children understand the relationship between 1,000s and 100s. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Understand partitioning of 4-digit numbers, including numbers with digits of 0. $5,000 + 60 + 8 = 5,068$ Understand and read 4-digit numbers on a number line.		
Choosing mental methods where appropriate	Use unitising and known facts to support mental calculations.  Make 1,405 from place value equipment.  Add 2,000.  Now add the 1,000s. 1 thousand + 2 thousands = 3 thousands  1,405 + 2,000 = 3,405	Use unitising and known facts to support mental calculations.  Th	Use unitising and known facts to support mental calculations. $4,256 + 300 = ?$ $2 + 3 = 5$ $200 + 300 = 500$ $4,256 + 300 = 4,556$		
Column addition with exchange	Use place value equipment on a place value grid to organise thinking.	Use place value equipment to model required exchanges.	Use a column method to add, including exchanges.		

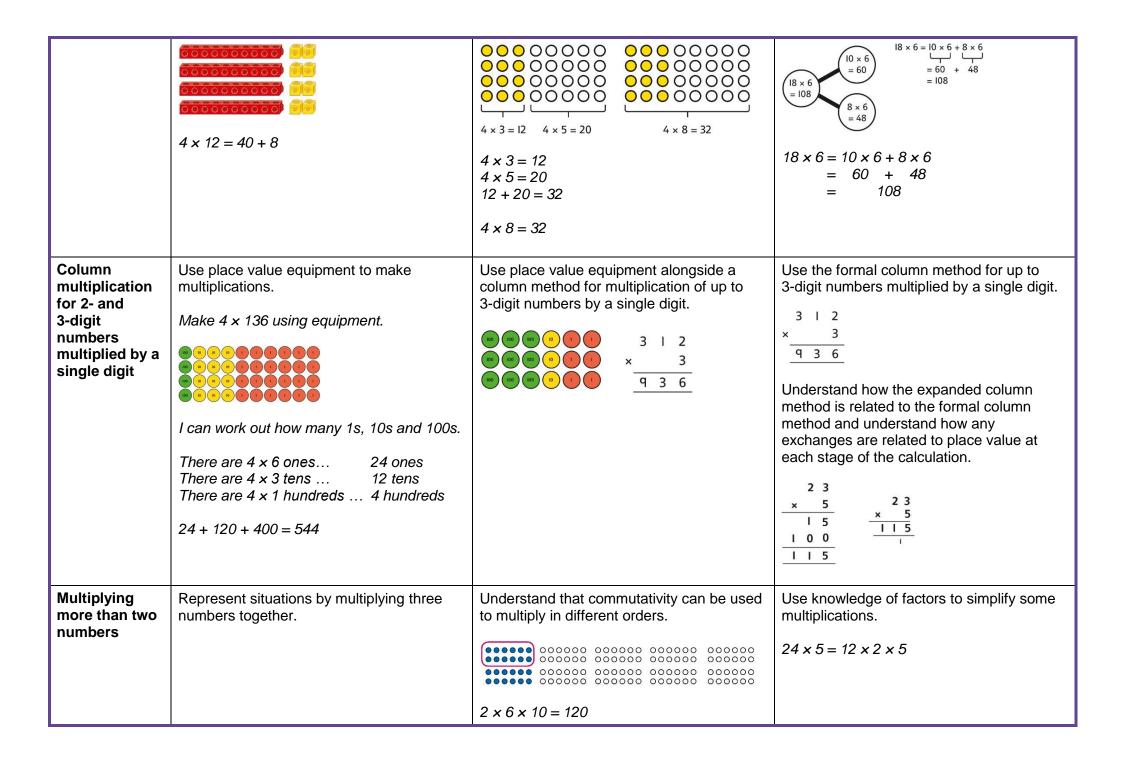
	Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers.	Th H T O	Th H T O 1 5 5 4 + 4 2 3 7
	Use equipment.to show 1,905 + 775.  The Heart Toology of the second row? Why is the Thousands box empty?  Which columns will total 10 or more?	Th H T O  Th H T T T O  Th H T T T O  Th H T T T T  Th H T T T T  Th H T T	Th H T O
Representing additions and checking strategies		Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate.	Use rounding and estimating on a number line to check the reasonableness of an addition.  10 1,000 2,000 3,000 4,000 5,000 6,000 7,000 8,000 9,000 10,000 912 + 6,149 = ?

		1,373 799 574 + 5 7 4 1 3 7 3	I used rounding to work out that the answer should be approximately 1,000 + 6,000 = 7,000.
		I chose to work out 574 + 800, then subtract 1.  6,000  2,999  3,001  This is equivalent to 3,000 + 3,000.	
Year 4 Subtraction		,	
Choosing mental methods where appropriate	Use place value equipment to justify mental methods.  What number will be left if we take away 300?	Use place value grids to support mental methods where appropriate.  Th	Use knowledge of place value and unitising to subtract mentally where appropriate.  3,501 - 2,000  3 thousands - 2 thousands = 1 thousand  3,501 - 2,000 = 1,501
Column subtraction with exchange	Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.	Represent place value equipment on a place value grid to subtract, including exchanges where needed.	Use column subtraction, with understanding of the place value of any exchange required.



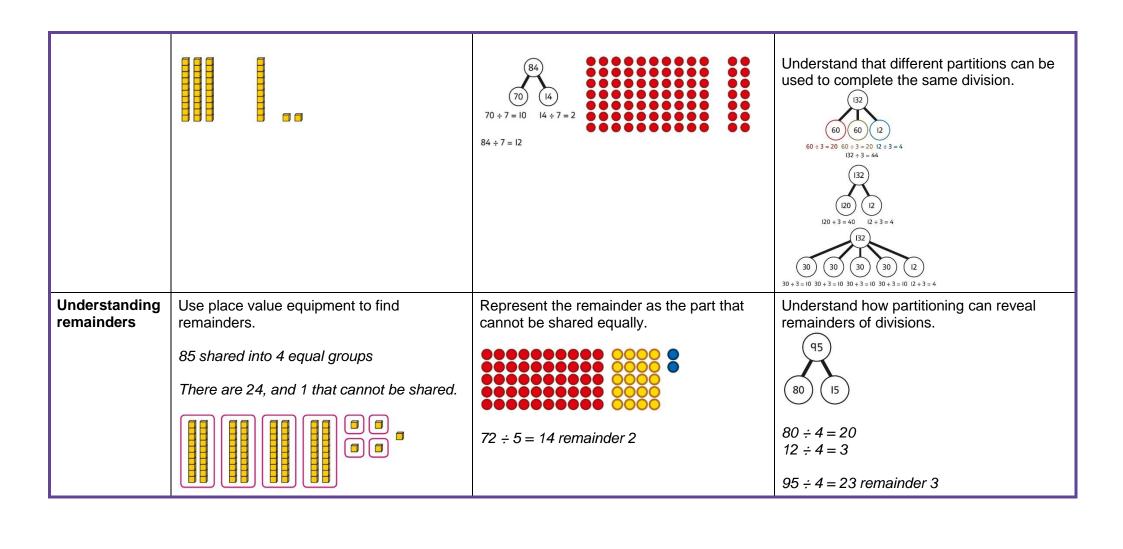


Multiplying by multiples of 10 and 100	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.	Use known facts and understanding of place value and commutativity to multiply mentally.
	3 groups of 4 ones is 12 ones. 3 groups of 4 tens is 12 tens. 3 groups of 4 hundreds is 12 hundreds.	$3 \times 4 = 12$ $3 \times 40 = 120$ $3 \times 400 = 1,200$	$4 \times 7 = 28$ $4 \times 70 = 280$ $40 \times 7 = 280$ $4 \times 700 = 2,800$ $400 \times 7 = 2,800$
Understanding times-tables up to 12 x 12	Understand the special cases of multiplying by 1 and 0.	Represent the relationship between the ×9 table and the ×10 table.	Understand how times-tables relate to counting patterns.
uρ ισ 12 x 12	$5 \times 1 = 5$ $5 \times 0 = 0$	Represent the $\times 11$ table and $\times 12$ tables in relation to the $\times 10$ table. $2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 11 = 40 + 4$	Understand links between the $\times 3$ table, $\times 6$ table and $\times 9$ table $5 \times 6$ is double $5 \times 3$ $\times 5$ table and $\times 6$ table I know that $7 \times 5 = 35$ so I know that $7 \times 6 = 35 + 7$ . $\times 5$ table and $\times 7$ table $3 \times 7 = 3 \times 5 + 3 \times 2$ $3 \times 5 \times $
Understanding and using partitioning in multiplication	Make multiplications by partitioning.  4 × 12 is 4 groups of 10 and 4 groups of 2.	Understand how multiplication and partitioning are related through addition.	6 × 9 = 60 - 6  Use partitioning to multiply 2-digit numbers by a single digit.  18 × 6 = ?



Voor	Each sheet has $2 \times 5$ stickers. There are $3$ sheets.  There are $5 \times 2 \times 3$ stickers in total. $5 \times 2 \times 3 = 30$ $10 \times 3 = 30$	$12 \times 10 = 120$ $10 \times 6 \times 2 = 120$ $60 \times 2 = 120$	12 × 2 × 5 =
Year 4 Division			
Understanding the relationship between multiplication and division, including times-tables	Use objects to explore families of multiplication and division facts.	Represent divisions using an array.	Understand families of related multiplication and division facts.  I know that $5 \times 7 = 35$ so I know all these facts: $5 \times 7 = 35$ $7 \times 5 = 35$ $35 = 5 \times 7$ $35 = 7 \times 5$ $35 \div 5 = 7$ $35 \div 7 = 5$ $7 = 35 \div 5$ $5 = 35 \div 7$
Dividing multiples of 10 and 100 by a single digit	Use place value equipment to understand how to use unitising to divide.	Represent divisions using place value equipment.	Use known facts to divide 10s and 100s by a single digit. $15 \div 3 = 5$ $150 \div 3 = 50$

Dividing Oak V	8 ones divided into 2 equal groups 4 ones in each group  8 tens divided into 2 equal groups 4 tens in each group  8 hundreds divided into 2 equal groups 4 hundreds in each group	$9 \div 3 = $ $10 \times 3 = $ $10 \times$	1500 ÷ 3 = 500
Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s	Partition into 10s and 1s to divide where appropriate. $39 \div 3 = ?$ $3 \times 10 = 30$ $3 \times 3 = 9$ $39 = 30 + 9$ $30 \div 3 = 10$ $9 \div 3 = 3$ $39 \div 3 = 13$	Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate. $39 \div 3 = ?$ 3 groups of 1 ten 3 groups of 3 ones $39 = 30 + 9$ $30 \div 3 = 10$ $9 \div 3 = 3$ $39 \div 3 = 13$	Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate. $142 \div 2 = ?$ $100 \div 2 = 40 \div 2 = 6 \div 2 = 1$ $100 \div 2 = 50$ $40 \div 2 = 20$ $6 \div 2 = 3$ $50 + 20 + 3 = 73$ $142 \div 2 = 73$
Dividing 2-digit and 3-digit numbers by a single digit, using flexible partitioning	Use place value equipment to explore why different partitions are needed.  42 ÷ 3 = ?  I will split it into 30 and 12, so that I can divide by 3 more easily.	Represent how to partition flexibly where needed.  84 ÷ 7 = ?  I will partition into 70 and 14 because I am dividing by 7.	Make decisions about appropriate partitioning based on the division required.  The partitioning based on the division required.



## **KEY STAGE 2**

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

**Key language:** decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

**Multiplication and division:** Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

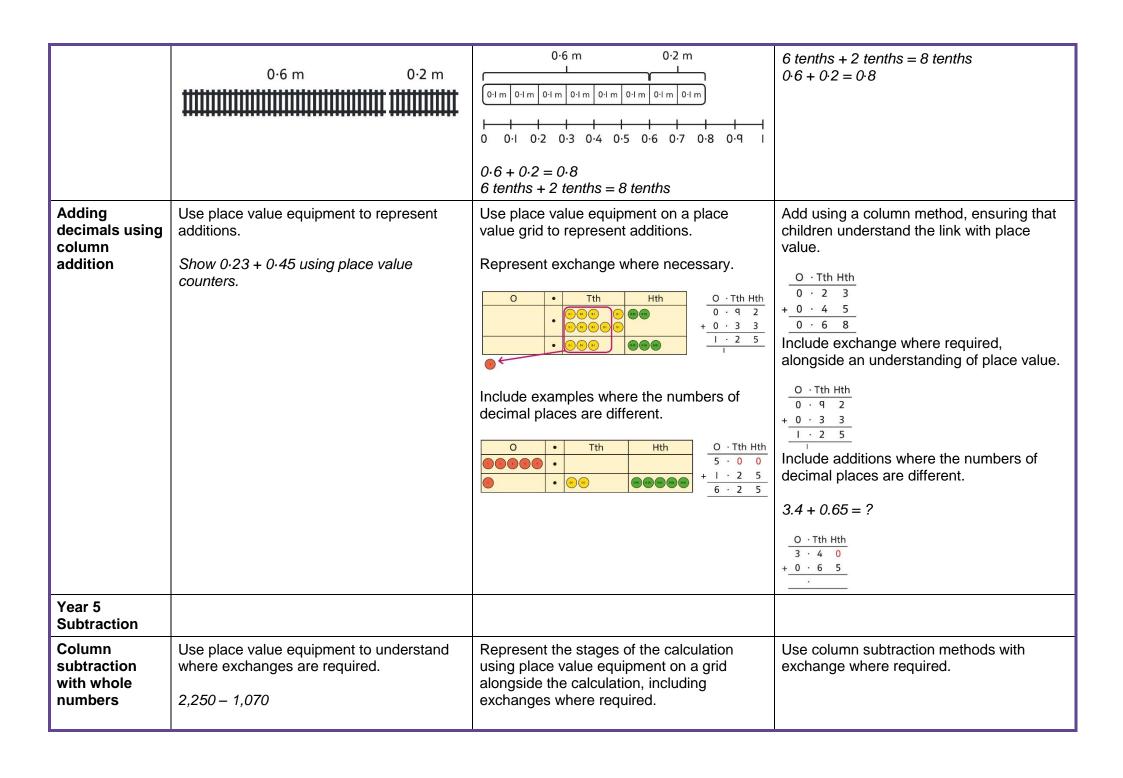
Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

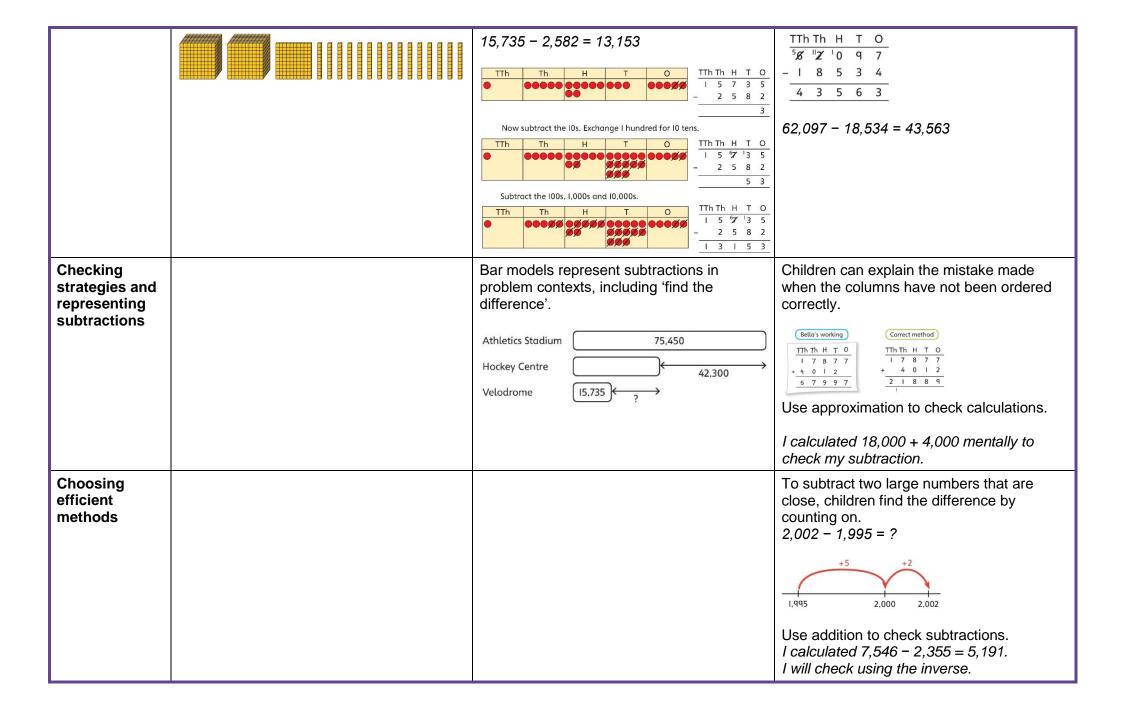
Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them. Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

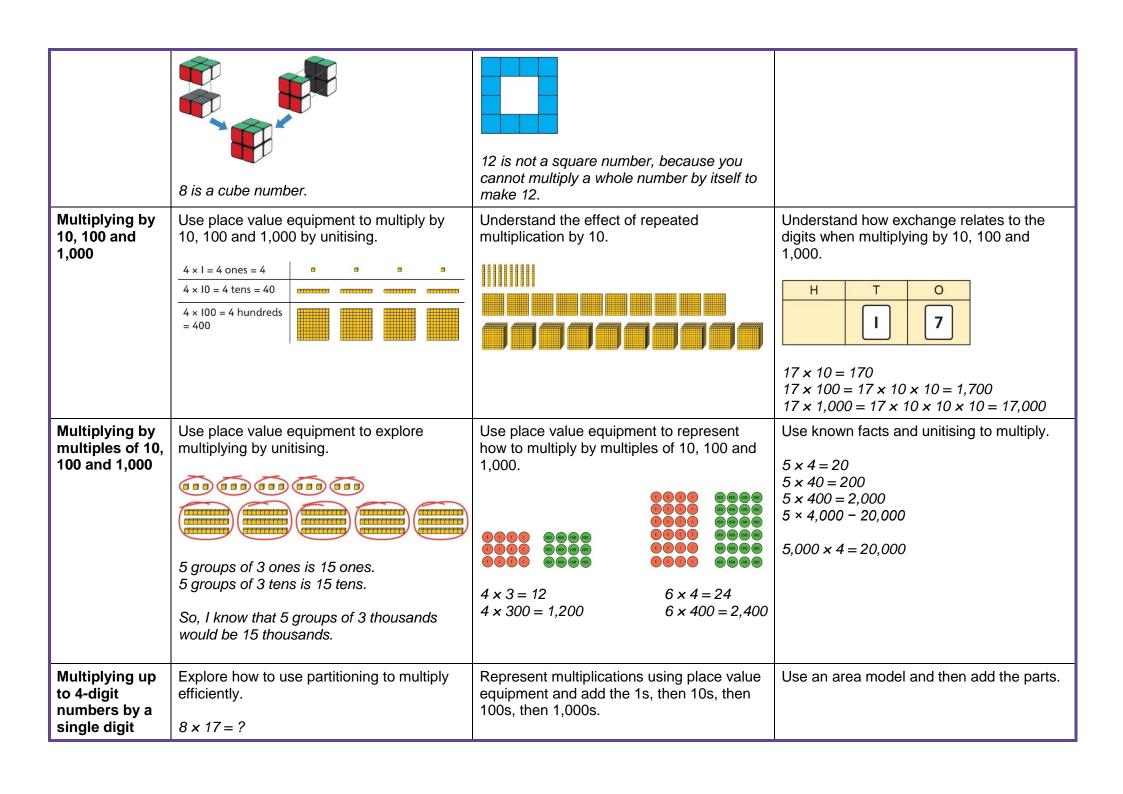
Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

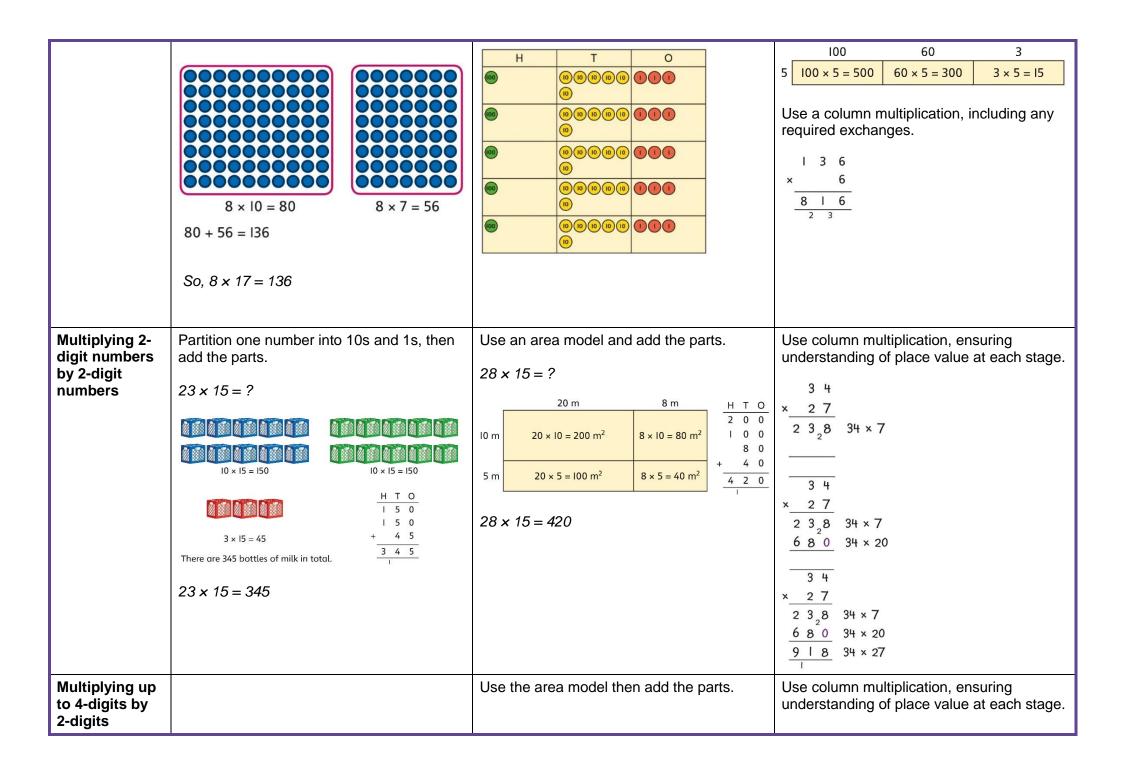
		Year 5	
	Concrete	Pictorial	Abstract
Year 5 Addition			
Column addition with whole numbers	Use place value equipment to represent additions.  Add a row of counters onto the place value grid to show 15,735 + 4,012.	Represent additions, using place value equipment on a place value grid alongside written methods.  TTh Th H T O O O O O O O O O O O O O O O O O O	Use column addition, including exchanges.    TTh Th
		The the to exchange to tens for a too.  The the true of the true o	
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving.	Use approximation to check whether answers are reasonable.    TTh Th
Adding tenths	Link measure with addition of decimals.  Two lengths of fencing are 0.6 m and 0.2 m.  How long are they when added together?	Use a bar model with a number line to add tenths.	Understand the link with adding fractions. $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$

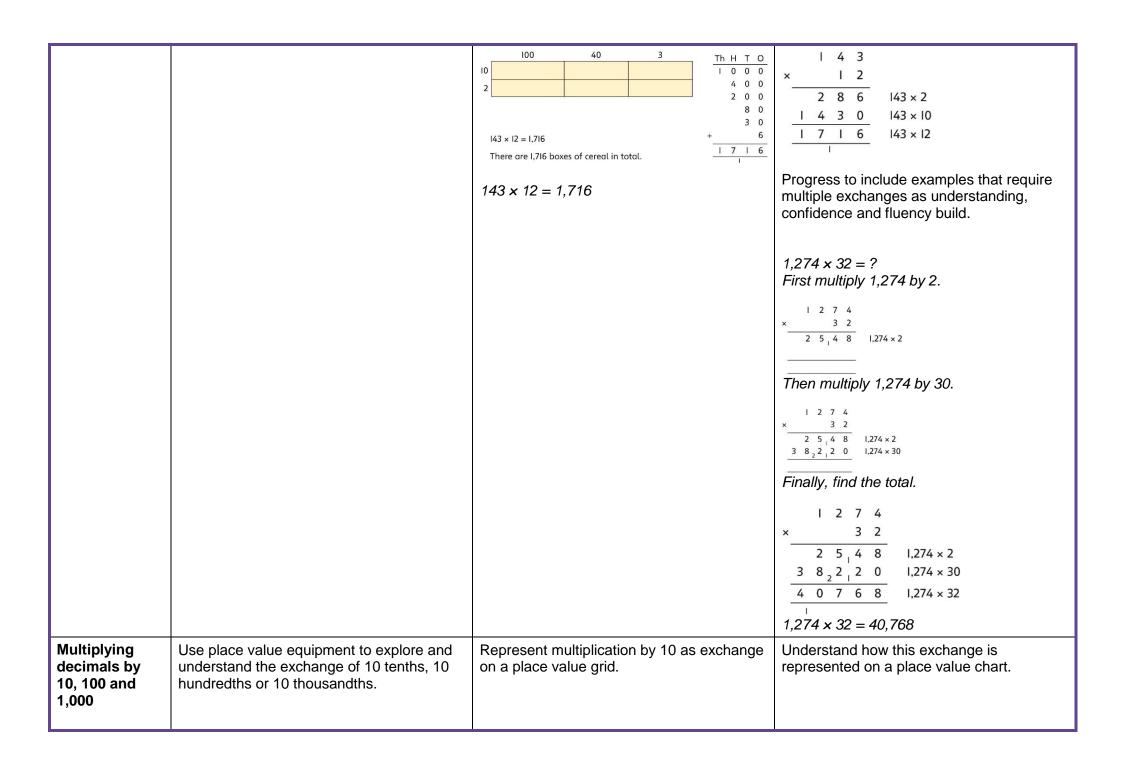




Subtracting decimals	Explore complements to a whole number by working in the context of length. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Use a place value grid to represent the stages of column subtraction, including exchanges where required. $5.74 - 2.25 = ?$ O Tth Hth $5.74 - 2.25 = ?$ Exchange I tenth for I0 hundredths.  O Tth Hth $5.6714 - 2.25 = ?$ Now subtract the 5 hundredths.  O Tth Hth $5.6714 - 2.25 = ?$ Now subtract the 5 hundredths.  O Tth Hth $5.6714 - 2.25 = ?$ Now subtract the 2 tenths, then the 2 ones.  O Tth Hth $5.6714 - 2.25 = ?$ Now subtract the 2 tenths, then the 2 ones.  O Tth Hth $5.6714 - 2.25 = ?$ Now subtract the 2 tenths, then the 2 ones.	Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.  3.921 - 3.75 = ?  O Tth Hth Thth 3 Q Q I - 3 7 5 0 - 3 7 5 0
Year 5 Multiplication		3 · 4 q	
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'.  25 is a square number because it is made from 5 rows of 5.  Use cubes to explore cube numbers.	Use images to explore examples and non-examples of square numbers. $8 \times 8 = 64$ $8^2 = 64$	Understand the pattern of square numbers in the multiplication tables.  Use a multiplication grid to circle each square number. Can children spot a pattern?



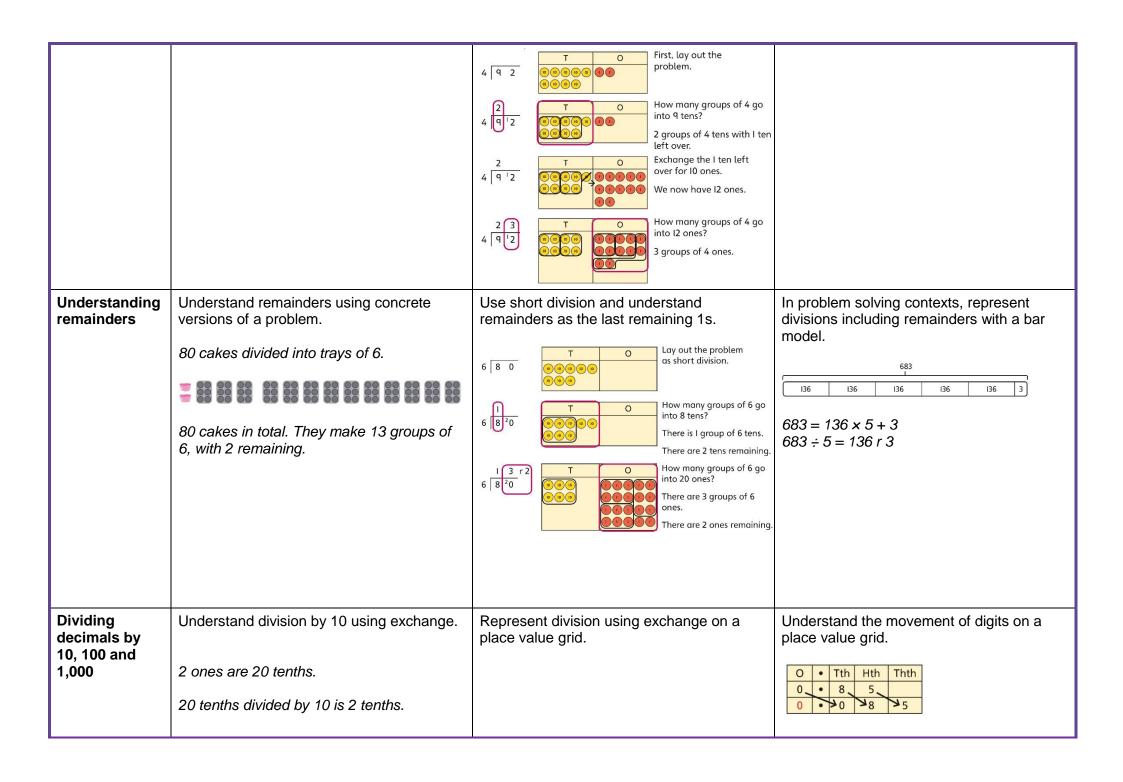




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Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number.	Understand that prime numbers are numbers with exactly two factors.	Understand how to recognise prime and composite numbers.
	24 ÷ 3 = 8 24 ÷ 8 = 3	$13 \div 1 = 13$ $13 \div 2 = 6 r 1$ $13 \div 4 = 4 r 1$	I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.
	8 and 3 are factors of 24 because they divide 24 exactly.	1 and 13 are the only factors of 13. 13 is a prime number.	I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.
	24 ÷ 5 = 4 remainder 4.		I know that 1 is not a prime number, as it has only 1 factor.
	5 is not a factor of 24 because there is a remainder.		
Understanding inverse operations and	Use equipment to group and share and to explore the calculations that are present.	Represent multiplicative relationships and explore the families of division facts.	Represent the different multiplicative relationships to solve problems requiring inverse operations.
the link with	I have 28 counters.	0000 0000 0000 0000	12 ÷ 3 =
multiplication, grouping and sharing	I made 7 groups of 4. There are 28 in total.	0000 0000 0000 0000	$\begin{vmatrix} 12 & + \\  &  \end{vmatrix} = 3$ $\times 3 =  2$ $\times 3$
	I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.	60 ÷ 4 = 15 60 ÷ 15 = 4	÷ 3 = 12

	I have 28 in total. I made groups of 4. There are 7 equal groups.		Understand missing number problems for division calculations and know how to solve them using inverse operations. $22 \div ? = 2$ $22 \div 2 = ?$ $? \div 2 = 22$ $? \div 22 = 2$
Dividing whole numbers by 10, 100 and	Use place value equipment to support unitising for division.	Use a bar model to support dividing by unitising.	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.
1,000	4,000 ÷ 1,000	380 ÷ 10 = 38    7	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
	4,000 is 4 thousands. 4 × 1,000= 4,000	10 ×	3,200 is 3 thousands and 2 hundreds. $200 \div 100 = 2$ $3,000 \div 100 = 30$ $3,200 \div 100 = 32$
	So, 4,000 ÷ 1,000 = 4	380 is 38 tens. 38 × 10 = 380 10 × 38 = 380 So, 380 ÷ 10 = 38	So, the digits will move two places to the right.
Dividing by multiples of 10, 100 and 1,000	Use place value equipment to represent known facts and unitising.	Represent related facts with place value equipment when dividing by unitising.	Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.
			$3,000 \div 5 = 600$ $3,000 \div 50 = 60$ $3,000 \div 500 = 6$
	15 ones put into groups of 3 ones. There are 5 groups. $15 \div 3 = 5$	180 is 18 tens.	$5 \times 600 = 3,000$ $50 \times 60 = 3,000$ $500 \times 6 = 3,000$
	15 tens put into groups of 3 tens. There are 5 groups.	18 tens divided into groups of 3 tens. There are 6 groups.  180 ÷ 30 = 6	
		100 7 30 = 0	

	150 ÷ 30 = 5	1	
Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment.  268 ÷ 2 = ?  There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones.  264 ÷ 2 = 134	Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting.   To O O O O O O O O O O O O O O O O O O O	Use short division for up to 4-digit numbers divided by a single digit. $ \begin{array}{cccccccccccccccccccccccccccccccccc$



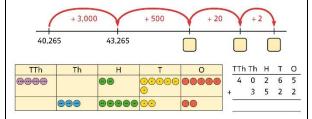
the relationship between fractions and division	fractions and division.  1 whole shared between 3 people. Each person receives one-third.	representations to show the link between fractions and division.  I $\div$ 3 = $\frac{1}{3}$ Year 6	to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$
Understanding	Use sharing to explore the link between	1.5 is 1 one and 5 tenths. This is equivalent to 10 tenths and 50 hundredths. 10 tenths divided by 10 is 1 tenth. 50 hundredths divided by 10 is 5 hundredths. 1.5 divided by 10 is 1 tenth and 5 hundredths. 1.5 ÷ 10 = 0.15  Use a bar model and other fraction	$8.5 \div 100 = 0.085$ Use the link between division and fractions

## Comparing and selecting efficient methods

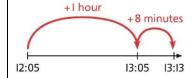
Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.

М	HTh	TTh	Th	Н	Т	0
•	••••	•	•	•••		•

Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.



Use bar model and number line representations to model addition in problem-solving and measure contexts.



Use column addition where mental methods are not efficient. Recognise common errors with column addition.

$$32,145 + 4,302 = ?$$

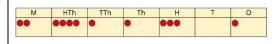
	TTh	Th	Н	Т	0	
	3	2	l	4	5	50)
+		4	3	0	2	
	3	6	4	4	7	

Which method has been completed accurately?

What mistake has been made?

Column methods are also used for decimal additions where mental methods are not efficient.

Selecting mental methods for larger numbers where appropriate Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.



2,411,301 + 500,000 = ?

This would be 5 more counters in the HTh place.

Use a bar model to support thinking in addition problems.

I added 100 thousands then subtracted 1 thousand.

Use place value and unitising to support mental calculations with larger numbers.

$$195,000 + 6,000 = ?$$

$$195 + 5 + 1 = 201$$

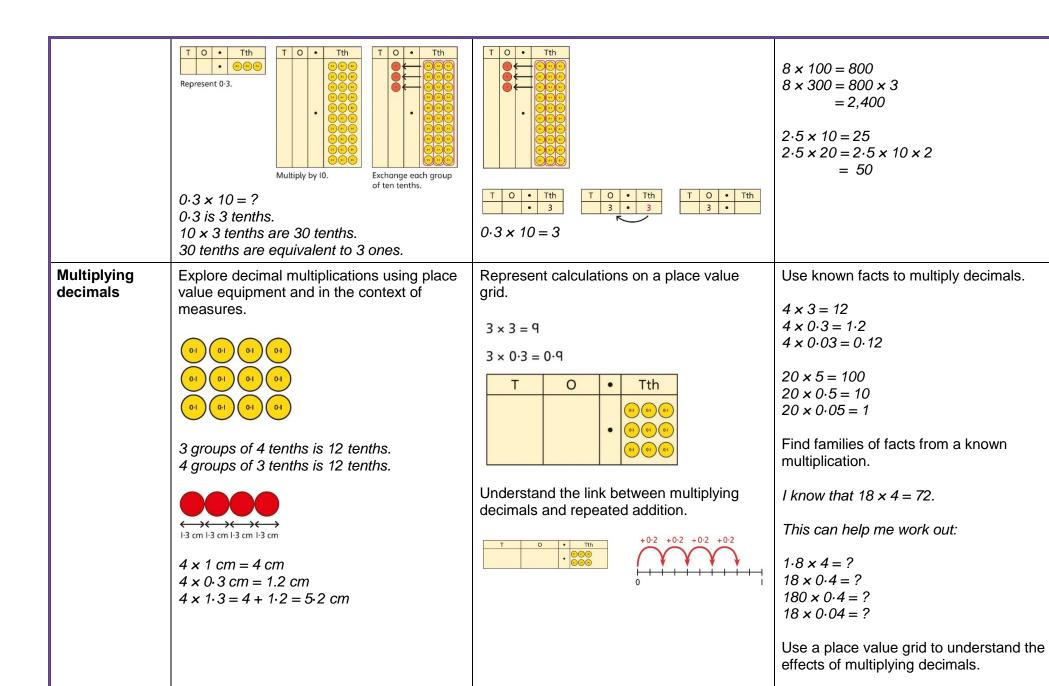
195 thousands + 6 thousands = 201 thousands

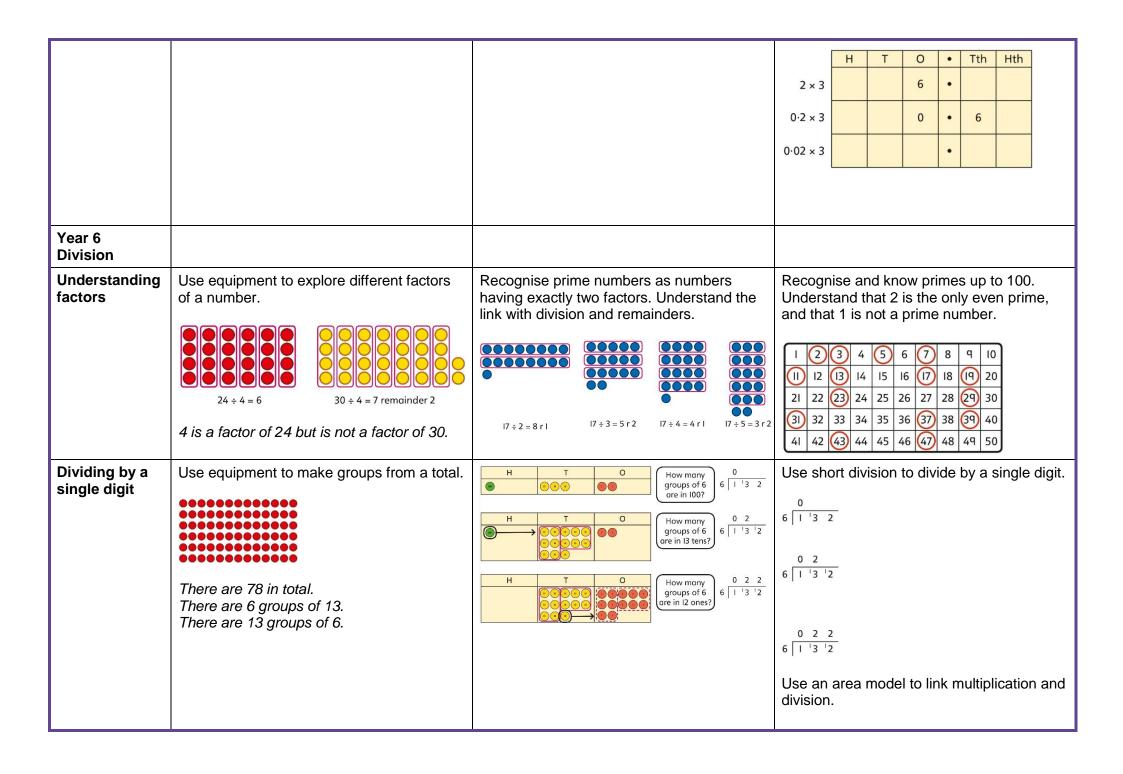
So, 
$$195,000 + 6,000 = 201,000$$

	So, the total is 2,911,301. 2,411,301 + 500,000 = 2,911,301	257 thousands + 100 thousands = 357 thousands 257,000 + 100,000 = 357,000 357,000 - 1,000 = 356,000 So, 257,000 + 99,000 = 356,000	
Understanding order of operations in calculations	Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$	Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Understand the correct order of operations in calculations without brackets.  Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ $4 + 96 = 100$ $(4 + 6) \times 16$ $10 \times 16 = 160$
Year 6 Subtraction			
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers.  The Head Counter of Larger numbers of Larger numbers.	Compare subtraction methods alongside place value representations.  Th H T O 2 6 7 9 - 5 3 4 2 1 4 5	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.   The Honor To Column Subtraction for decimal problems, including in the context of measure.

		Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.   computer game  puzzle book  fl2-50	H T O · Tth Hth 3 0 9 · 6 0 - 2 0 6 · 4 0 1 0 3 · 2 0
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations.  950,000 - 150,000  That is 950 thousands - 150 thousands  950,000 - 800 thousands. 950,000 - 150,000 = 800,000	Subtract efficiently from powers of 10.  10,000 - 500 = ?
Year 6 Multiplication			
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications.  Th T O O O O O O O O O O O O O O O O O O	Use place value equipment to compare methods.    Method	Understand area model and short multiplication.  Compare and select appropriate methods for specific multiplications.  Method 3  3,000 200 20 5 4 12,000 800 80 20 12,000 + 800 + 80 + 20 = 12,900  Method 4  3 2 2 5  × 4  1 2 9 0 0  1 2

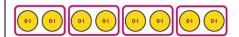
Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication.  Method I  1,000 200 30 5  20 20,000 4,000 600 100  1 1,000 200 30 5  × 2 1  5 1×5  3 0 1×30  2 0 0 1×200  1 0 0 0 1×1,000  1 0 0 20×5  6 0 0 20×30  4 0 0 0 20×200  2 0 0 0 0 20×1,000  2 5 9 3 5 21×1,235	Use compact column multiplication with understanding of place value at all stages.    1 2 3 5
Using knowledge of factors and partitions to compare methods for multiplications	Use equipment to understand square numbers and cube numbers. $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.  20 5.200 × 20 5.200 × 25 5.2	Use a known fact to generate families of related facts.    170 × II
Multiplying by 10, 100 and 1,000	Use place value equipment to explore exchange in decimal multiplication.	Understand how the exchange affects decimal numbers on a place value grid.	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000.





Dividing by a 2-digit number	Understand that division by factors can be used when dividing by a number that is not	Use factors and repeated division.	?   10   10   1   1   6   132   6   60   60   6   6   6   6   6   6	
using factors	prime.	1,260 $\div$ 14 = ? 1,260 $\div$ 2 = 630 630 $\div$ 7 = 90 1,260 $\div$ 14 = 90	$2,100 \div 12 = ?$ $2,100 \rightarrow \underbrace{\begin{array}{c} +2 \\ -2,100 \rightarrow \underbrace{\begin{array}{c} +2 \\ -2,100 \rightarrow \underbrace{\begin{array}{c} +6 \\ -2,100 \rightarrow \underbrace{\begin{array}{c} +3 \\ -2,100 \rightarrow \underbrace{\begin{array}{c} +4 \\ -2,100 \rightarrow \underbrace{\begin{array}$	
Dividing by a 2-digit number using long division	Use equipment to build numbers from groups.  182 divided into groups of 13. There are 14 groups.	Use an area model alongside written division to model the process. $377 \div 13 = ?$	Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process. $377 \div 13 = ?$ $0  13  26  39  52  65  78  91  104  117  130  $	

			A slightly different layout may be used, with the division completed above rather than at the side.  3 21 7 9 8 - 6 3 0 1 6 8  21 7 9 8 - 6 3 0 1 6 8 - 1 6 8 0  Divisions with a remainder explored in
Dividing by 10, 100 and 1,000	Use place value equipment to explore division as exchange.	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	problem-solving contexts.  Use knowledge of factors to divide by multiples of 10, 100 and 1,000. $40 \div 50 = \bigcirc$ $40 \longrightarrow \div 10 \longrightarrow \div 5 \longrightarrow ?$ $40 \longrightarrow \div 5 \longrightarrow \div 10 \longrightarrow ?$ $40 \div 5 = 8$ $8 \div 10 = 0.8$ $So, 40 \div 50 = 0.8$
Dividing decimals	Use place value equipment to explore division of decimals.	Use a bar model to represent divisions.	Use short division to divide decimals with up to 2 decimal places.



8 tenths divided into 4 groups. 2 tenths in each group.

0.8							
?	?	?	?				

 $4 \times 2 = 8$ 

 $8 \div 4 = 2$ 

So,  $4 \times 0.2 = 0.8$   $0.8 \div 4 = 0.2$ 

0 · 5 3 8 4 · 42 24